Method used	Data used	Conclusions

# GEOMAGNETIC EXCITATION OF NUTATION

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Introduction	Method used	Data used	Conclusions
Introduction			

- Atmospheric and oceanic excitations play dominant role in polar motion and rotational velocity of the Earth.
- Thanks to the precise P/N model IAU2000/2006, small but non-negligible effects can be seen also in the celestial pole offsets (CPO), i.e. in nutation.
- These effects are caused by quasi-diurnal changes of angular momentum functions of the geophysical fluids (atmosphere, oceans,..)

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Motivation			

- In our previous study we found that atmospheric/oceanic effects do not explain the observed celestial pole offsets (CPO) completely.
- The integrated excitations in CRF in comparison with the observed CPO became out-of-phased after some period.
- We suppose that other excitations have effect. We tested the epochs of strong earthquakes, and geomagnetic jerks (Malkin, 2013),
  - GMJ rapid changes of the secular variations of geomagnetic field.
- Re-initialization of the integration in the dates of these events was used and
- the best agreement has been found for the GMJ epochs.
- But the re-initialization of integration is not acceptable from the physical point of view.
- Here we present a different approach adding a continuous excitation near GMJ epochs.

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Method used		

# Broad-band Liouville equations

- The excitations of the Earth rotation in the celestial reference frame (nutation) by atmosphere and ocean were studied using
- Brzezinski's broad-band Liouville equations (1994)

$$\ddot{P} \quad -i(\sigma'_{\mathcal{C}} + \sigma'_{f})\dot{P} - \sigma'_{\mathcal{C}}\sigma'_{f}P = -\sigma_{\mathcal{C}}\left\{\sigma'_{f}(\chi'_{p} + \chi'_{w}) + \sigma'_{\mathcal{C}}(a_{p}\chi'_{p} + a_{w}\chi'_{w}) + i[(1 + a_{p})\dot{\chi}'_{p} + (1 + a_{w})\dot{\chi}'_{w}]\right\}$$

where

- P = dX + idY is excited motion of Earth's spin axis in celestial frame (CRF).
- $\sigma'_{C}$ ,  $\sigma'_{f}$  are the complex Chandler and FCN frequencies in CRF, respectively,  $\sigma_{C}$  in TRF.
- $a_p = 9.200 \times 10^{-2}$ ,  $a_w = 2.628 \times 10^{-4}$  are dimensionless constants (Koot & de Viron, 2011).
- $\chi'_p$  and  $\chi'_w$  are the angular momentum excitation functions (presure and wind) expressed in CRS

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Method used			

- To be able to integrate the system we need initial values  $P_0$ ,  $\dot{P}_0$  constrained so that the free Chandlerian term (with quasi-diurnal period in celestial frame) vanishes.
- The initial values are closely connected to the phase and amplitude of the integrated series.
- The final choice of  $P_0$  was made by repeating integration with different values  $P_0$  to fit the integrated series to VLBI observations so that reaches a minimum rms differences,

	Method used	Data used	Conclusions
Method u	ised		
Procedure of s	earching the additiona	Levoitations	

• Geomagnetic jerks (or secular geomagnetic variation impulse) is a relatively sudden change in the second derivative of the Earth's magnetic field with respect to time. (Olsen & Mandea, 2007).



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## Method used

Integration with simulated schematic excitation



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	Method used	Data used	Conclusions
Method u	sed		
Procedure of s	earching the additional	excitations	

- We fix the the central epochs of additional excitations around GMJ epochs:
  - 1991.0, 1994.0, 1999.0, 2003.5, 2004.7, and 2007.5.
- GMJs last typically several months.
- The length of excitation was fixed to 200 days.
- The complex amplitudes of the excitations were estimated to lead to the best rms fit to observed CPO.
- In our previous studies we also tested if the excitations is preceeding, delaying or corresponding to the GMJ epochs
- The best agreement was found for the epochs of GMJ.

	Method used	Data used	Conclusions
Data used			
Celestial pole offsets			

- Celestial pole offsets
  - The last IVS combined solution ivs14X1q.eoxy covering the interval 1989.0-2014.0. *dX* and *dY* are given in unequally spaced intervals.
  - then the empirical Sun-synchronous correction of IAU2000 nutation model has been added in order to be the observed CPO comparable with the atmospheric contribution.
  - than the series were filtered to retain only periods between 60 and 6000 days and interpolated at regular 10-day intervals and.

Observed and filtered (60<P<6000d)



	Method used	Data used	Conclusions
Data used			
Atmospheric angul	or momentum		

- There are two sources of Atmospheric angular momentum data
  - European Centre for Medium-Range Weather Forecasts (ECMWF), ERA40
  - Atmospheric and Environmental Research, USA, NCEP/NCAR reanalysis
- Our previous study based on AAM/OAM function of European meteorological Center ECMWF ERA40 and on the ocean model OMCT showed not so good agreement in comparison with the NCEP/NCAR series.
- No model of oceanic angular momentum driven by NCEP atmosphere is available for the whole period
- The pressure term with IB correction a simple model of oceanic response on the pressure changes.

	Method used	Data used	Conclusions
Data used			
Atmospheric an	gular momentum		

- The time series of AAM  $\chi$  (complex values) were transformed from the terrestrial frame to the celestial frame by using the complex decomposition at retrograde diurnal frequency  $\chi' = -\chi e^{i\Phi}$ ,  $\Phi$  is the Greenwich sidereal time.
- Because we are interested in the long-periodic motion (comparable with nutation), we applied the smoothing to remove periods shorter than 10 days and calculated their time derivatives needed for integration.

	Method used	Data used	Results	Conclusions
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#### Results

#### pressure term with IB correction



# Comparison of integrated series with the observed celestial pole offsets.



Results Wavelet based semblance analysis

Cooper & Cowan, 2008



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Geomagnetic excitation of nutation

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### Wavelet based semblance analysis



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Conclusions			

- Geophysical excitations can yield significant contribution to nutation, of the order of 0.1mas;
- NCEP solution with the inverted barometer correction leads to better agreement than ERA solution
- The application of schematic additional excitations at GMJ epochs improves the agreement of integrated pole position with VLBI observations.
- The interpretation of the physical nature of the GMJ effect on nutation requires more study in future.